

Relation between critical current degradation due to pressure in magnets and experimental data

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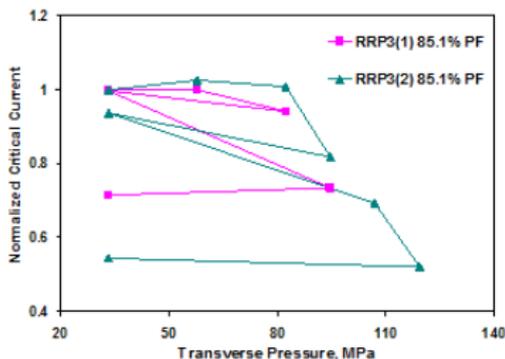
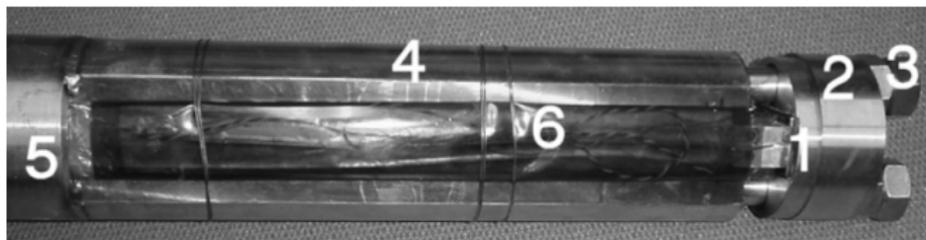


Outline

- 1 Experimental setup
- 2 Comparison between experimental data and magnet behaviour
- 3 ANSYS model of the experiment
 - Choice of the model
 - Effect of radial stress
 - Effect of thermal loads
- 4 Further developments



FNAL Experimental setup

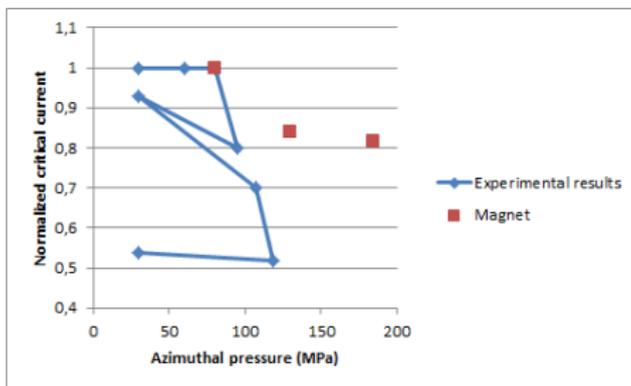


The cable is pressed along transverse direction (i.e. azimuthal in magnets) and critical current is measured.

* "A Device to Test Critical Current Sensitivity of Nb₃Sn Cables to Pressure", E. Barzi, M. Fratini, A. V. Zlobin. *Advances in Cryogenic Engineering*, V. 48, AIP, V. 614, pp. 45-52 (2002).
 * "Effect of Transverse Pressure on Brittle Superconductors", E. Barzi, D. Turrioni, and A. V. Zlobin. *IEEE Trans. Appl. Sup.*, V. 18, No. 2, p. 980 (2008).



Experimental results



Magnet data are plotted against maximum azimuthal stress in the magnet during pre-load.

Experimental data don't seem to be consistent with magnet ones.



Goal of the work

Original goal

Find an **equivalent quantity** using a simple analytical model that predicts the behaviour of the magnet.

Problem

Inhomogeneity and anisotropy of the cable make it challenging to produce a single equivalent parameter.



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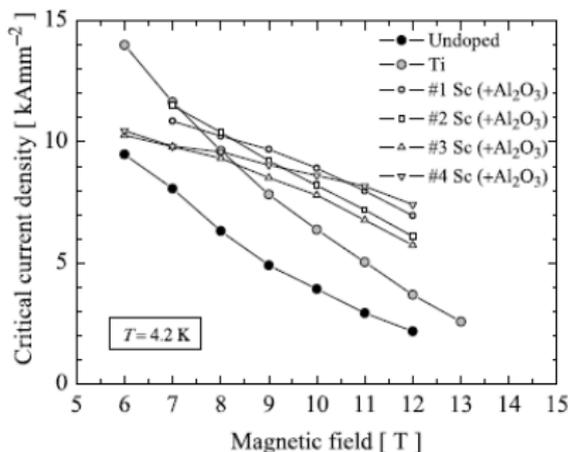
New goals

- See how **different loads** can affect the current degradation.
- Try to **modify the experimental setup** in order to improve experimental data.

* Marco Danuso's Laurea Thesis - 2008, Sant'Anna School, Pisa: "*Parametric Analysis of Forces and Stresses in Superconducting Magnets Windings*", M. Beghini, A. Zlobin, E. Barzi advisors.



Current degradation due to magnetic field



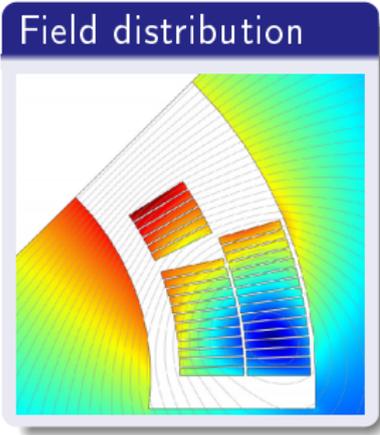
Critical current decreases rapidly with magnetic field.

Bottleneck should be where the magnetic field is higher.

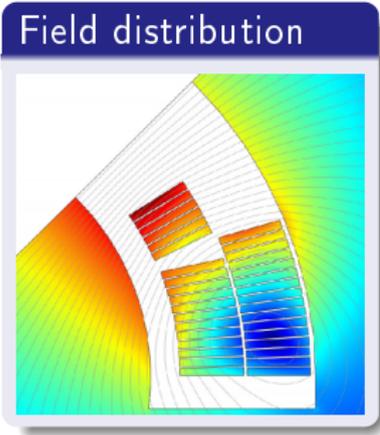
* "Nb₃Sn research and development in the USA - Wires and cables", D.R. Dietderich, A. Godeke.



Field and stress distribution on the magnet



Field and stress distribution on the magnet

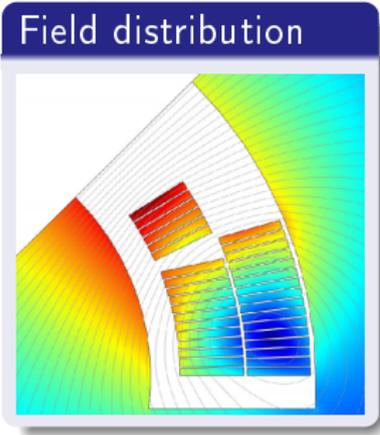


* *"Magnetic Mirror Structure for Testing Shelltype Quadrupole Coils"*, N. Andreev, E. Barzi, R. Bossert, G. Chlachidze, V. S. Kashikhin, V. V. Kashikhin, M. J. Lamm, F. Nobrega, I. Novitski, M. Tartaglia, D. Turrioni, R. Yamada, A. V. Zlobin.

- Magnetic field is high at the pole.
- Critical current bottleneck will be at the pole.
- We must look at stress at the pole.



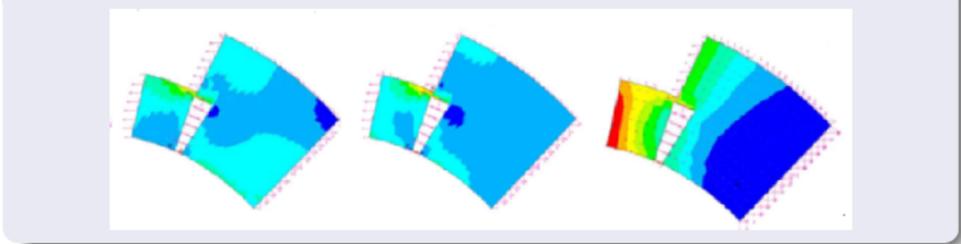
Field and stress distribution on the magnet



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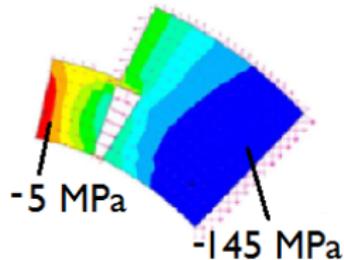
- Magnetic field is high at the pole.
- Critical current bottleneck will be at the pole.
- We must look at stress at the pole.

Stress distribution: 300 K, 4.5 K, powered magnet



Stress in the magnet

* "The Study of Single Nb3Sn Quadrupole Coils Using a Magnetic Mirror Structure", G. Chlachidze et al., IEEE Trans. Appl. Sup., V. 21, No. 3, p. 1692 (2011).



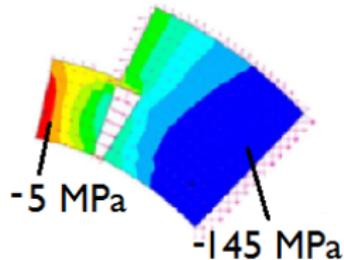
Powered magnet

- Small loads on the pole.
- No reversible degradation.
- No permanent degradation.



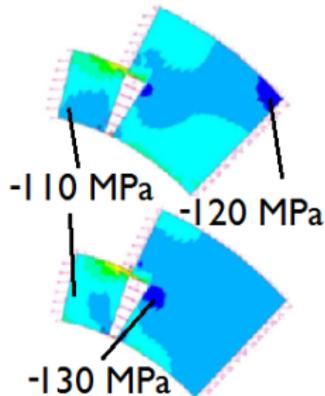
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Powered magnet

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Pre-loaded magnet

- No reversible degradation.
- Loads on the pole are higher than before.
- The highest load is still not at the pole.



Comparing magnet behaviour with experimental data

Conclusion

- The interesting degradation is the **permanent** one, because there will not be any reversible degradation in the powered pole.
- Test results must be compared with the stress reached on the **pole** during pre-load.

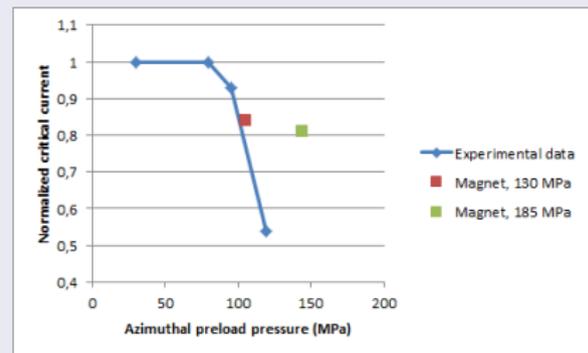


Comparing magnet behaviour with experimental data

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Permanent degradation

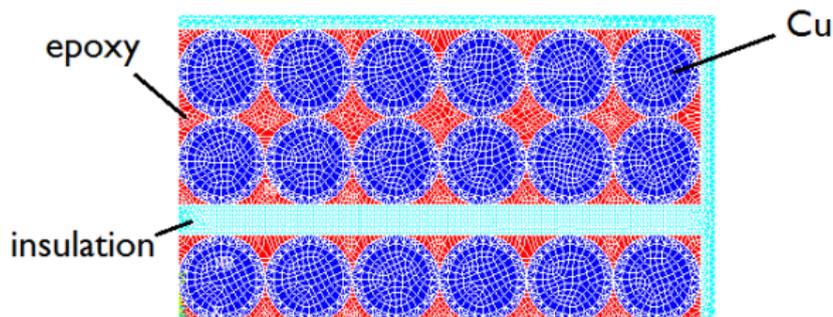
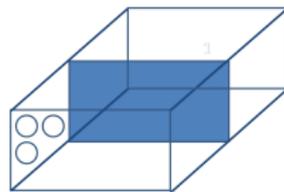


Magnet data are plotted against maximum stress reached where the field is maximum.



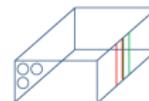
Ansys model

- **2D** model of the section.
- Elastic materials.
- No contact elements between strands.



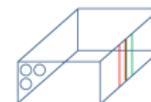
Choice of the elements

In order to choose the correct 2D model, we have to evaluate the behaviour of the sample in axial direction.

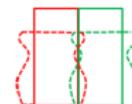


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In order to choose the correct 2D model, we have to evaluate the behaviour of the sample in axial direction.



Plane stress does not keep the integrity of the material.

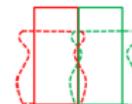


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Plane stress does not keep the integrity of the material.



Plane strain does not allow the material to deformate in the axial direction.

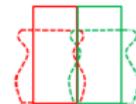


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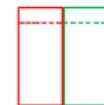
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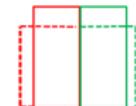
Plane stress does not keep the integrity of the material.



Plane strain does not allow the material to deformate in the axial direction.



Generalized plane strain forces the axial strain to be constant on the whole section but it does not force it to be zero.



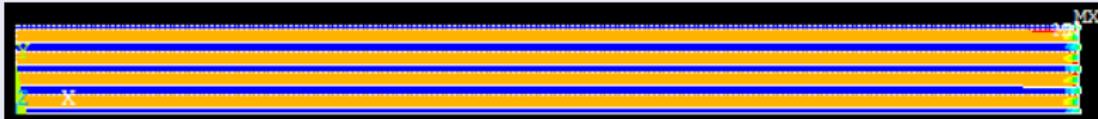
Verification of the model

Simple ANSYS model of an orthogonal section.



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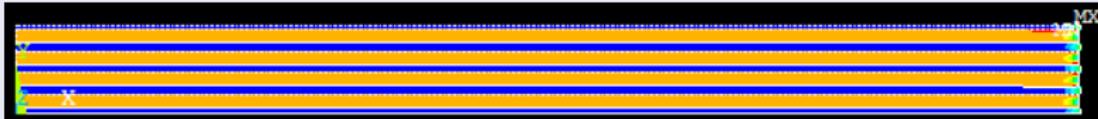


Axial stress is not constant, so plane stress is not correct.



Verification of the model

Simple ANSYS model of an orthogonal section.



Axial stress is not constant, so plane stress is not correct.



Axial strain is constant (and not zero) along the section, as in the generalized plane strain assumption.



Effect of radial stress

Stress simulated

for $i = 0$ to 15, for $j = 0$ to 15: $\sigma_{\theta\theta} = 10 \cdot i$ MPa, $\sigma_{rr} = 10 \cdot j$ MPa

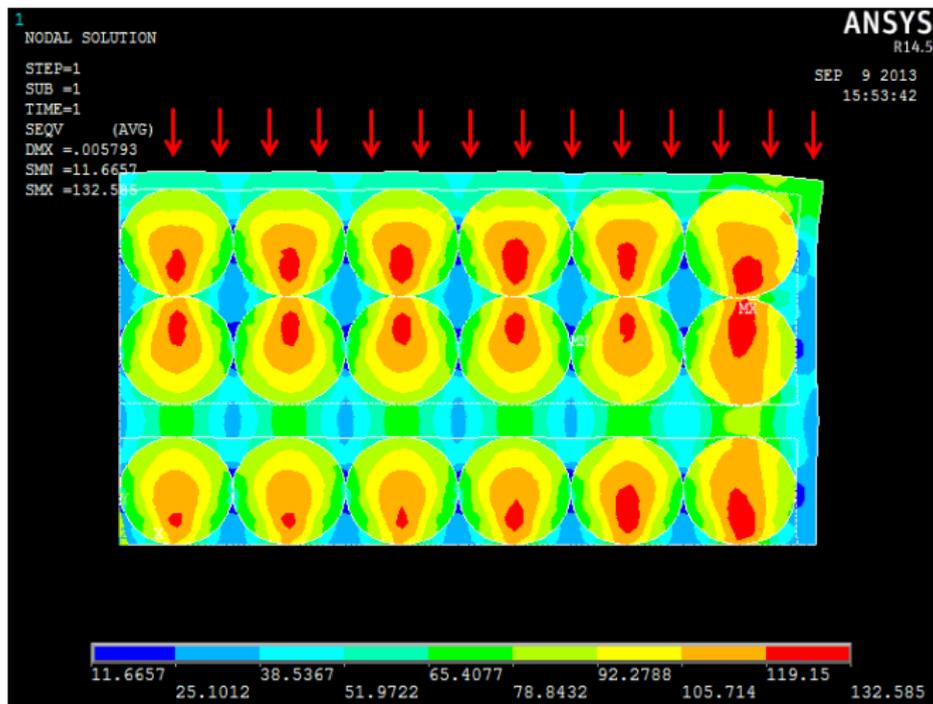
Von Mises plots shown

- 1 $\sigma_{\theta\theta} = 80$ MPa, $\sigma_{rr} = 0$
- 2 $\sigma_{\theta\theta} = 80$ MPa, $\sigma_{rr} = 40$ MPa



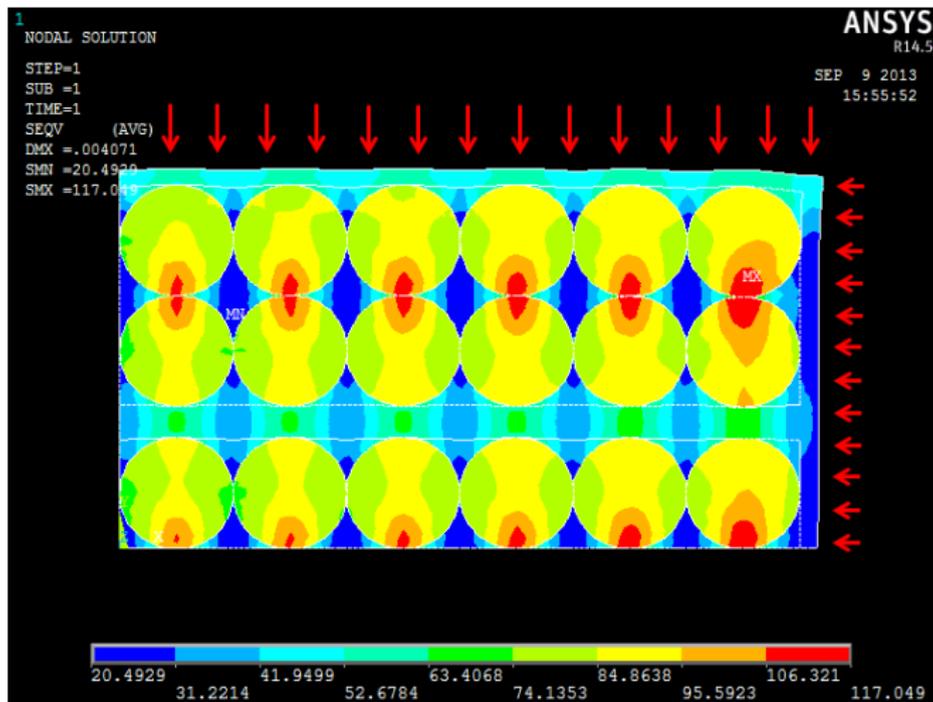
Effect of radial stress

$$\sigma_{\theta\theta} = 80 \text{ MPa}, \sigma_{rr} = 0$$

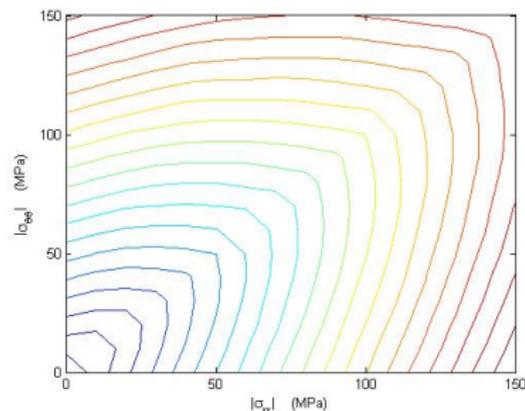
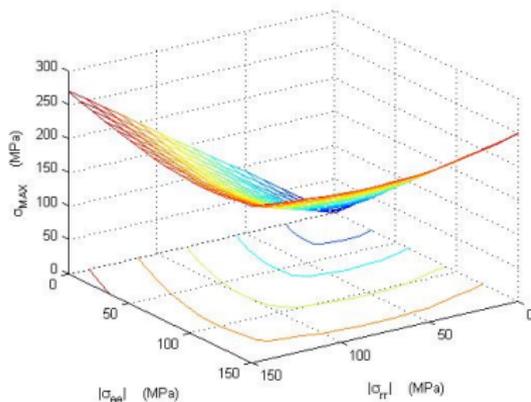


Effect of radial stress

$$\sigma_{\theta\theta} = 80 \text{ MPa}, \sigma_{rr} = 40 \text{ MPa}$$



Effect of radial stress

Summary: $\sigma_{MAX}(\sigma_{rr}, \sigma_{\theta\theta})$ 

Maximum Von Mises stress in the strand while coupling azimuthal and radial stresses is lower than when having no radial stress.



Summary of different configurations results

Configuration	σ_{MAX}	$\sigma_{MAX,or}$	Observations
Epoxy voids	~ 150 MPa	133 MPa	Singularities
Compact strands	126 MPa	133 MPa	Low stress in center
Compact strands, voids	~ 150 MPa	133 MPa	Singularities
Nb_3Sn strands	137 MPa	133 MPa	
Side azimuthal load	139 MPa	133 MPa	
Central azimuthal load	135 MPa	133 MPa	
Partial radial load	124 MPa	117 MPa	



Effect of thermal loads

Results can be incorrect if **thermal loads** are not considered

Different materials in a compound subjected to a temperature variation must expand or contract in the same way, and this induces stress.



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Different materials in a compound subjected to a temperature variation must expand or contract in the same way, and this induces stress.

Cable as epoxy-copper compound

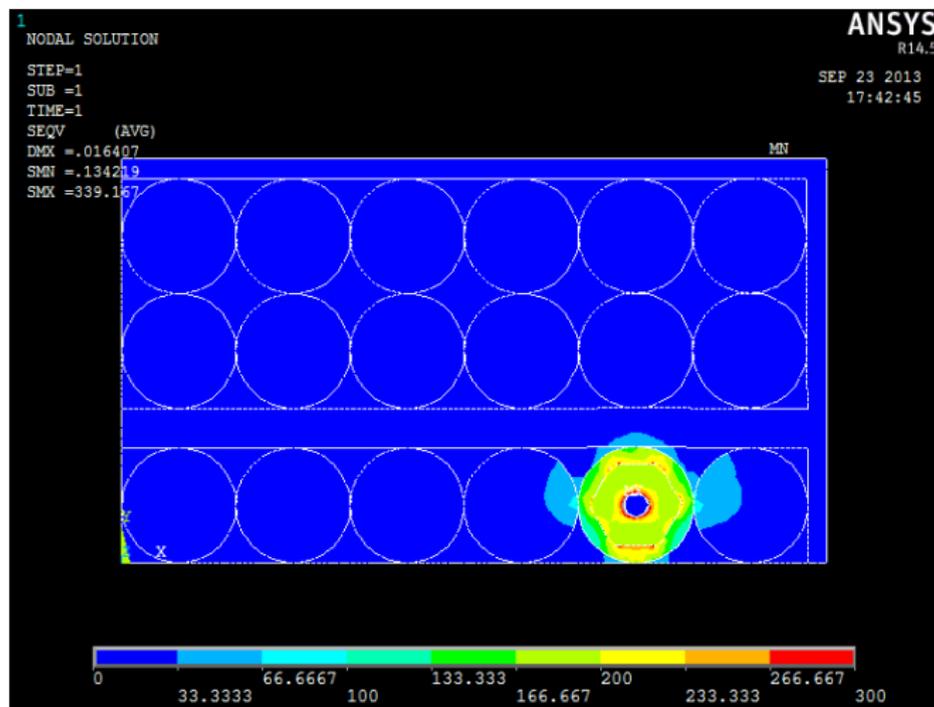
Epoxy can not withstand high tensile stress caused by differential contraction; it is going to break locally and follow the deformation of the copper.

Strand as copper- Nb_3Sn compound

Different thermal expansion coefficient between copper and Nb_3Sn can bring high loads on the material after lowering the temperature.

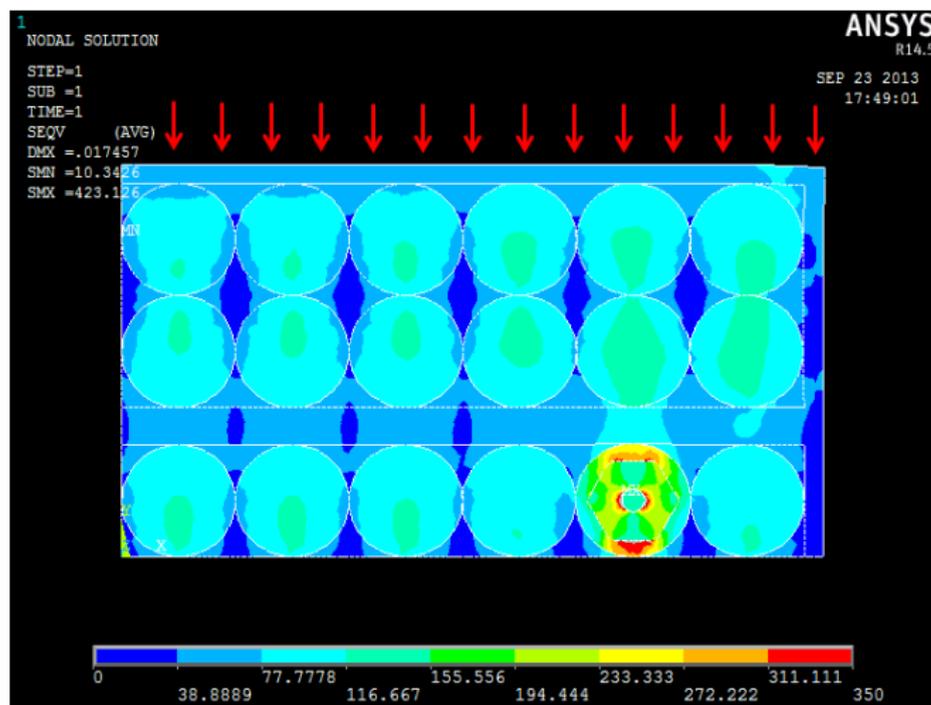


Effect of thermal loads

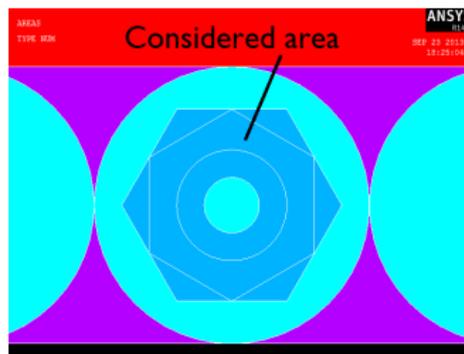
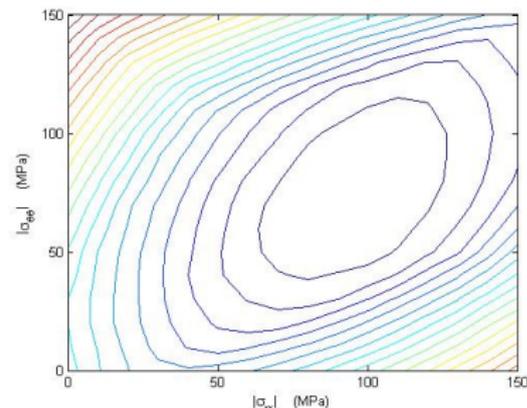
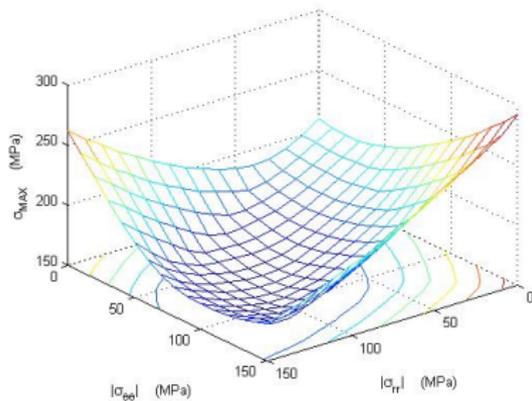
Copper- Nb_3Sn thermal loads

Effect of thermal loads

Mechanical and thermal loads



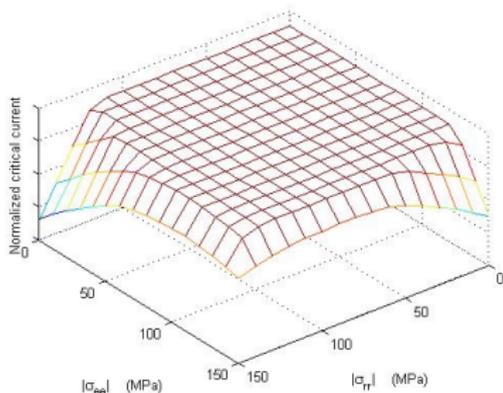
Effect of thermal loads

Summary: $\sigma_{MAX}(\sigma_{rr}, \sigma_{\theta\theta})$ with thermal loads

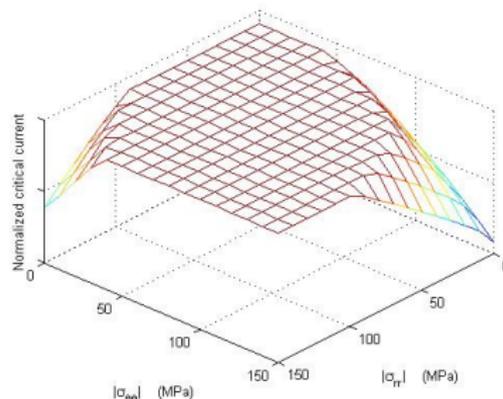
Effect of thermal loads

Qualitative prevision of critical current degradation

Warm preload

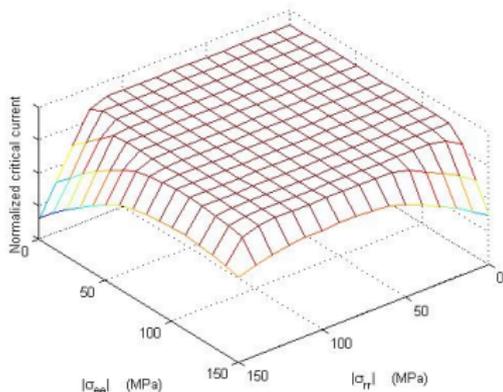


Cold preload

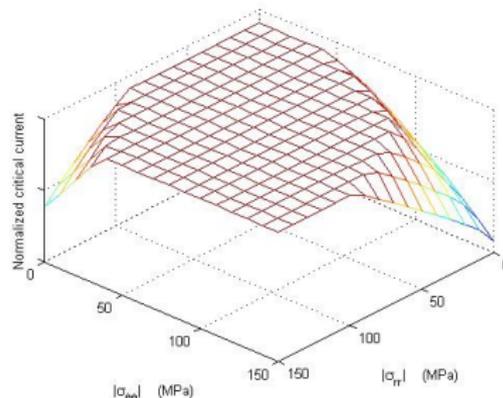


Qualitative prevision of critical current degradation

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Cold preload



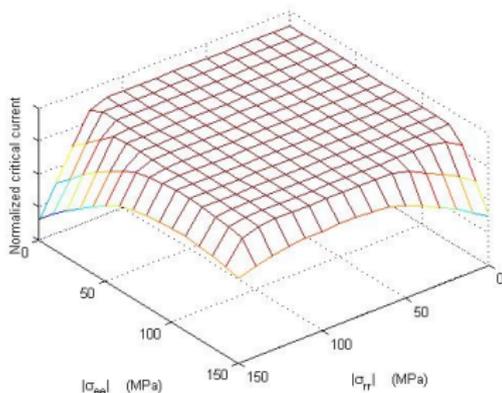
Hypothesis

- 1 Degradation depends on local Von Mises stress values

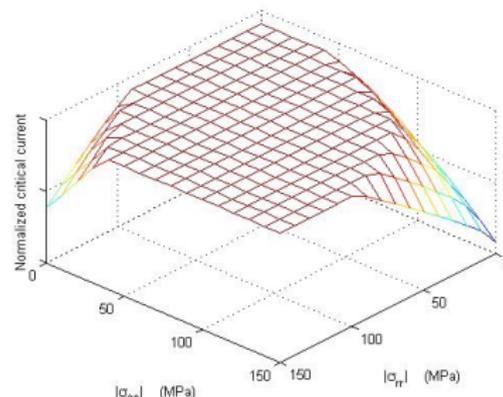


Qualitative prevision of critical current degradation

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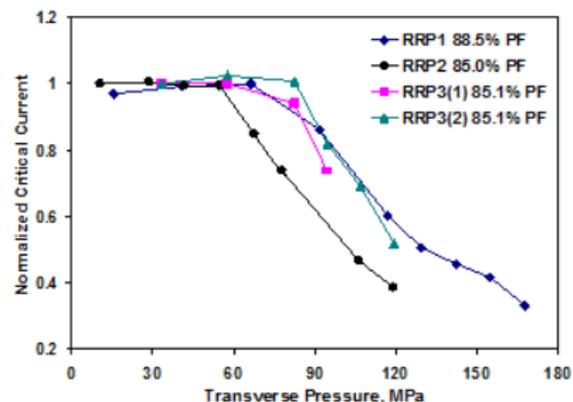
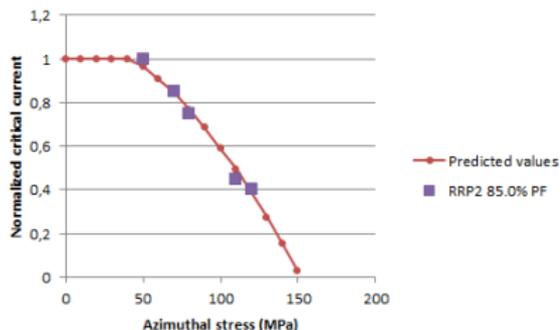
- ① Degradation depends on local Von Mises stress values
- ② Stress values lower than maximum stress reached in Nb_3Sn at 4.2 K do not give degradation



Fitting on experimental data

Hypothesis

- 1 $I_c = k\sigma_{MAX} + q$
- 2 $I_c(\sigma_{MAX}(0, 0, 4.2K)) = 1$



Further developments

- Try to modify the experimental set up.
- Study the differences between applying load at room temperature or after cooling down.
- Study the effect of radial stress and map permanent degradation in terms of both radial and azimuthal stress.



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